Course Syllabus

I. General Information

| Course name | Calculus II |
|--|-------------|
| Programme | Mathematics |
| Level of studies (BA, BSc, MA, MSc, long-cycle | BA |
| MA) | |
| Form of studies (full-time, part-time) | Full-time |
| Discipline | Mathematics |
| Language of instruction | English |

| Course coordinator/person responsible | dr Andrzej Michalski |
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| course coordinator/person responsible | ai / iiiai zej iviieiiaisiti |

| Type of class (use only the types mentioned below) | Number of teaching hours | Semester | ECTS Points |
|--|--------------------------|----------|-------------|
| lecture | 60 | III | 10 |
| tutorial | | | |
| classes | 60 | III | |
| laboratory classes | | | |
| workshops | | | |
| seminar | | | |
| introductory seminar | | | |
| foreign language | | | |
| classes | | | |
| practical placement | | | |
| field work | | | |
| diploma laboratory | | | |
| translation classes | | | |
| study visit | | | |

| Course pre-requisites | Calculus I |
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II. Course Objectives

To present the basic concepts and theorems in calculus of several variables.

To develop skills in applied calculus of several variables.

III. Course learning outcomes with reference to programme learning outcomes

| Symbol | | Reference to | |
|--------|--|--------------------|--|
| | Description of course learning outcome | programme learning | |
| | | outcome | |
| | KNOWLEDGE | | |
| W_01 | Basic concepts and definitions of calculus of several variables | K_W01, K_W02, | |
| | (K_W01, K_W02, K_W03, K_W04, K_W05, K_W07). | K_W03, K_W04, | |
| | | K_W05, K_W07 | |
| W_02 | Basic methods and theorems of calculus of several variables | K_W01, K_W02, | |
| | (K_W01, K_W02, K_W03, K_W04, K_W05, K_W07). | K_W03, K_W04, | |
| | | K_W05, K_W07 | |
| W_03 | Selected applications of calculus of several variables (K_W01, | K_W01, K_W02, | |
| | K_W02, K_W03, K_W04, K_W05, K_W07). | K_W03, K_W04, | |
| | | K_W05, K_W07 | |
| | SKILLS | | |
| U_01 | Solve typical problem using standard methods (K_U01, K_U02, | K_U01, K_U02, | |
| | K_U03, K_U04, K_U05, K_U06, K_U10, K_U12, K_U13, K_U14, | K_U03, K_U04, | |
| | K_U15). | K_U05, K_U06, | |
| | | K_U10, K_U12, | |
| | | K_U13, K_U14, | |
| | | K_U15 | |
| U_02 | Analyze complex problem, propose and explain the optimal | K_U01, K_U02, | |
| | methods for its solution (K_U01, K_U02, K_U03, K_U04, | K_U03, K_U04, | |
| | K_U05, K_U06, K_U10, K_U12, K_U13, K_U14, K_U15). | K_U05, K_U06, | |
| | | K_U10, K_U12, | |
| | | K_U13, K_U14, | |
| | | K_U15 | |
| U_03 | Solve selected practical problems (K_U01, K_U02, K_U03, | K_U01, K_U02, | |
| | K_U04, K_U05, K_U06, K_U10, K_U12, K_U13, K_U14, K_U15). | K_U03, K_U04, | |
| | | K_U05, K_U06, | |
| | | K_U10, K_U12, | |
| | | K_U13, K_U14, | |
| | | K_U15 | |
| | SOCIAL COMPETENCIES | | |
| K_01 | Formulate and present opinions on the applicability of calculus | K_K01, K_K05 | |
| | methods taking into account own knowledge and skills (K_K01, K_K05). | _ | |

IV. Course Content

Continuity and differentiability of functions of several variables. Higher order derivatives. Local and global extreme values. Implicit function. Local invertibility. Extreme values of an implicit function. Lagrange coefficients method. Mappings in Cartesian spaces. Multiple integrals. Iterated integrals. Change of variables. Line integrals. Green's theorem. Surface integrals. Divergence (Gauss-Ostrogradsky) theorem. Stokes theorem. Applications.

V. Didactic methods used and forms of assessment of learning outcomes

| | 1 | | |
|--------|------------------------|--------------------------|--------------------------|
| Symbol | Didactic methods | Forms of assessment | Documentation type |
| | (choose from the list) | (choose from the list) | (choose from the list) |
| | | KNOWLEDGE | |
| W_01 | conventional lecture, | test, written exam, oral | evaluated test, protocol |
| | discussion, practical | exam | |
| | classes | | |
| W_02 | conventional lecture, | test, written exam, oral | evaluated test, protocol |
| _ | discussion, practical | exam | |
| | classes | | |
| W_03 | conventional lecture, | test, written exam, oral | evaluated test, protocol |
| _ | discussion, practical | exam | |
| | classes | | |
| | | SKILLS | |
| U_01 | conventional lecture, | test, written exam, oral | evaluated test, protocol |
| | discussion, practical | exam | |
| | classes | | |
| U_02 | conventional lecture, | test, written exam, oral | evaluated test, protocol |
| _ | discussion, practical | exam | |
| | classes | | |
| U_03 | conventional lecture, | test, written exam, oral | evaluated test, protocol |
| _ | discussion, practical | exam | |
| | classes | | |
| | | SOCIAL COMPETENCIES | |
| K_01 | conventional lecture, | test, written exam, oral | evaluated test, protocol |
| _ | discussion, practical | exam | |
| | classes | | |
| 1 | | | |

VI. Grading criteria, weighting factors.....

LECTURE:

The completion of classes is required. Written and oral exam together constitute the final grade (after each semester):

91 - 100% excellent

81 - 90% very good

71 - 80% good

61 - 70% satisfactory

51 - 60% sufficient

less than 51% fail

CLASSES:

At least 80% of attendance is required. Two tests together constitute the final grade (each semester):

91 - 100% excellent

81 - 90% very good

71 – 80% good

61 - 70% satisfactory

51 - 60% sufficient

less than 51% fail

Detailed assessment rules are given during lectures and classes.

VII. Student workload

| Form of activity | Number of hours |
|--|---|
| Number of contact hours (with the teacher) | Lecture: 60 hrs. |
| | Classes: 60 hrs. |
| | Individual consultations: 30 hrs. |
| | In total: 150 hrs. |
| Number of hours of individual student work | Preparation for classes: 60 hrs. |
| | Studying books: 45 hrs. |
| | Preparation for tests and exams: 45 hrs |
| | In total: 150 hrs. |

VIII. Literature

| Basic literature | |
|-----------------------|--|
| Lecture notes. | |
| Worksheets. | |
| Additional literature | |

In English:

- R. Ellis, D. Gulick, Calculus: One and Several Variables, Harcourt Brace Jovanovich, 1991.
- D. D. Berkey, P. Blanchard, Calculus, Saunders College Pub., 1992.
- S. L. Salas, E. Hille, J. T. Anderson, Calculus: One and Several Variables with Analytic Geometry, Wiley, 1986.

In Polish:

- W. Rudin, Podstawy analizy matematycznej, PWN, Warszawa 2002.
- M. Gewert, Z. Skoczylas, Analiza Matematyczna 2, Oficyna Wydawnicza GiS, 2005.
- M. Gewert, Z. Skoczylas, Elementy analizy wektorowej. Teoria, przykłady, zadania., Oficyna Wydawnicza GiS, 2012.
- W. Krysicki, L. Włodarski, Analiza matematyczna w zadaniach, PWN, 2004.
- J. Banaś, S. Wędrychowicz, Zbiór zadań z analizy matematycznej, WNT, Warszawa 1996.
- G. Fichtenholz, Rachunek różniczkowy i całkowy, PWN, 2005.